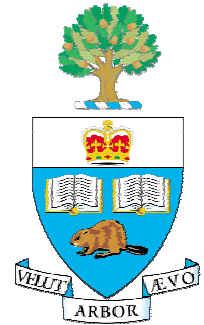




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# Mapping Multiplexers onto Hard Multipliers in FPGAs

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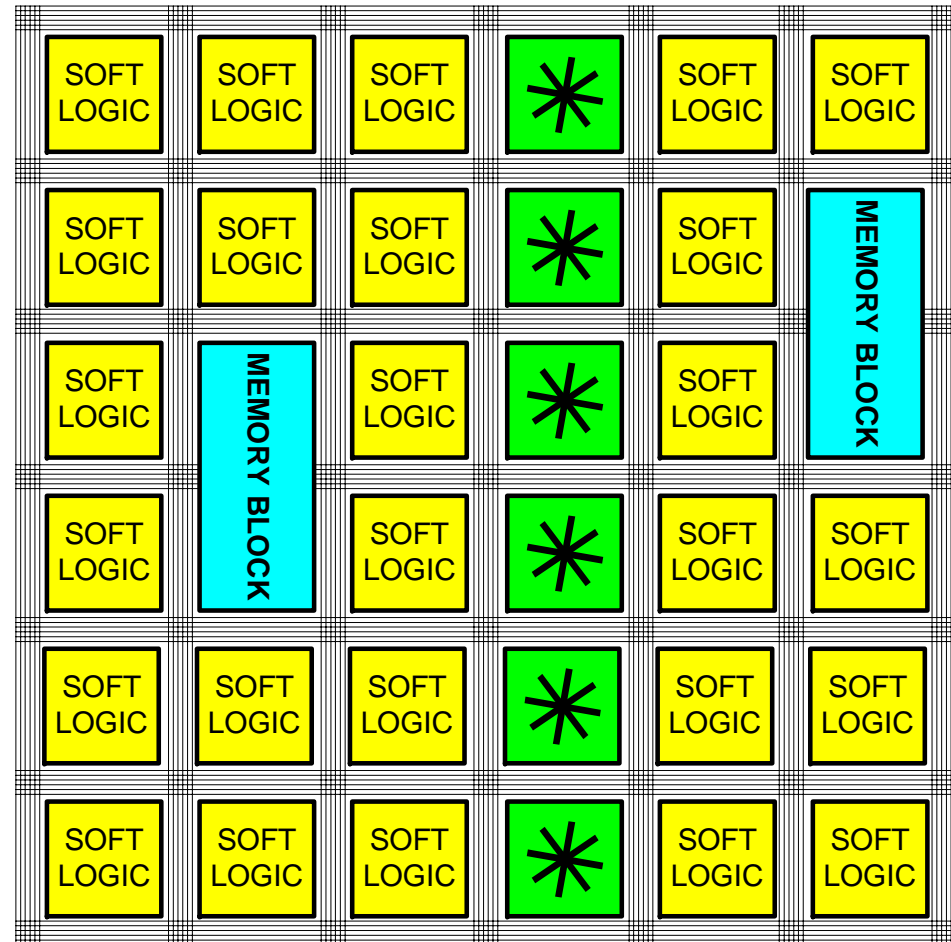
University of Toronto



# Modern FPGAs

Consist of:

1. Programmable logic and routing
  - **soft logic fabric**
2. Less-programmable dedicated circuits
  - **hard structures**
  - e.g. multiplier
  - e.g. memory block





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# FPGA Hard Structures

- Are very useful **when used**
  - major gain in speed, logic density
- Are very **wasteful when not used**
- The logic area goes unused, but worse...





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# Programmable Routing is Wasted!

- 70%-90% of FPGA area is routing!
- Everyone pays for hard structures
  - but not everyone can use all of them





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# What can we do about waste?

Try to employ unused hard structures

1. Use multiplier as barrel shifter
  - [Gigliotti, 2004]
2. Use memory block as lookup table to implement combinational logic
  - [Wilton, 2002; Cong and Xu, 2000]





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# Our Idea

- Employ unused multipliers to implement **multiplexers**
  - Saves programmable logic
- Multiplexers are common in many applications:
  - Networking
  - Processors
  - Many kinds of datapath





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# How to Make Multiplexers from Multipliers

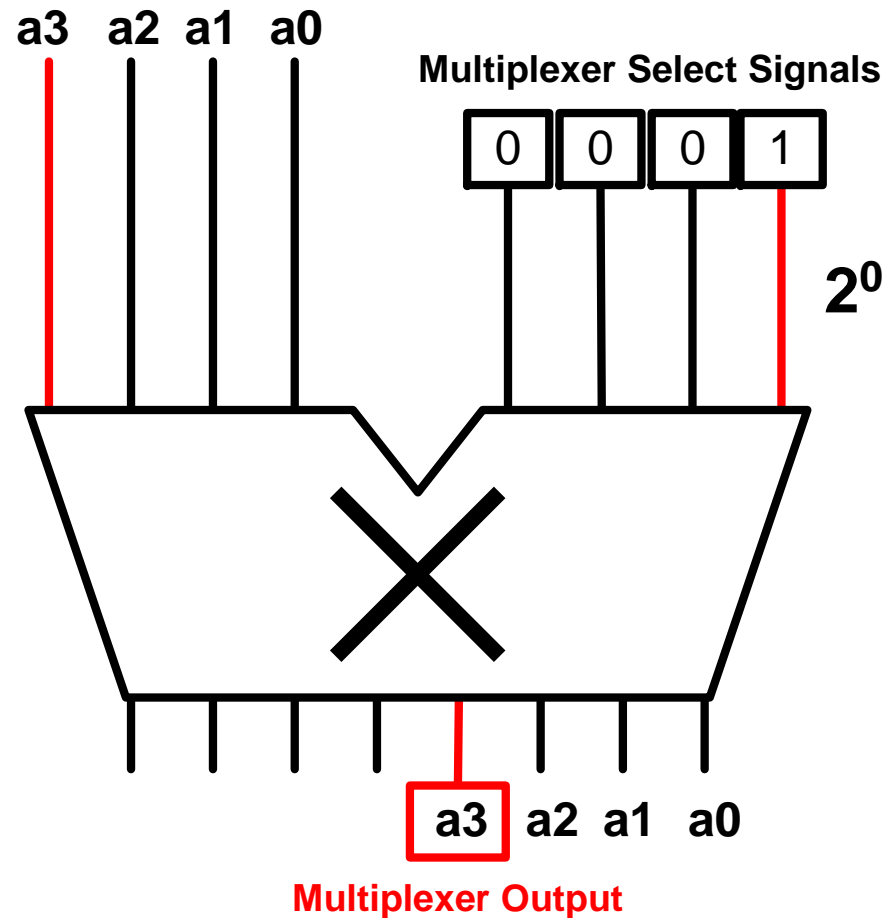
Recall:

- multiply a number by  $2^n$  shifts the binary number by **n** bit positions
- we're going to use it to make expensive shifters/multiplexers
  - Not actually expensive, since multiplier was going unused!



# Use Multiplier to Shift/Select

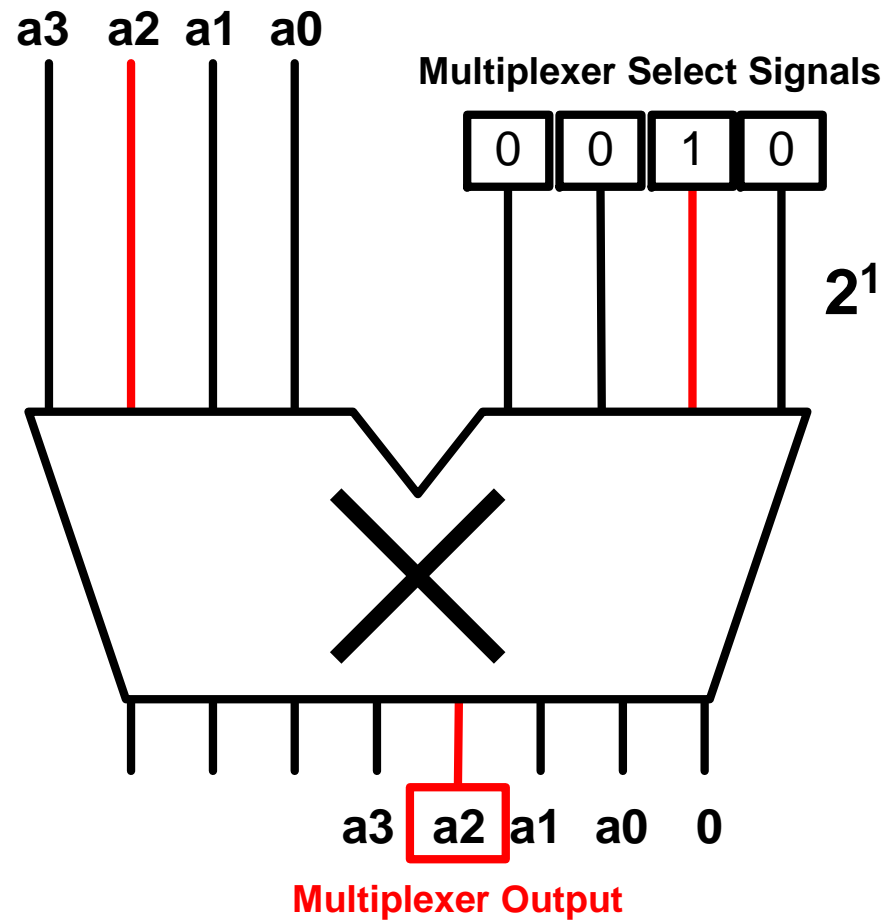
- Use shift to select input to pass through





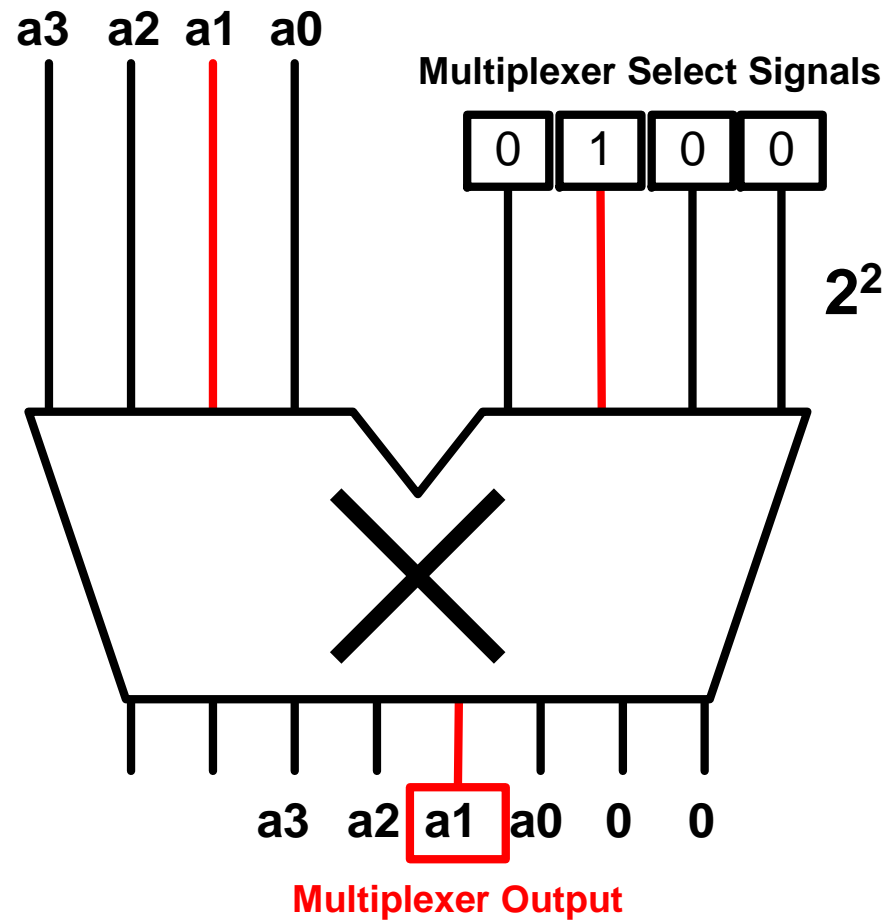
# Use Multiplier to Shift/Select

- Use shift to select input to pass through



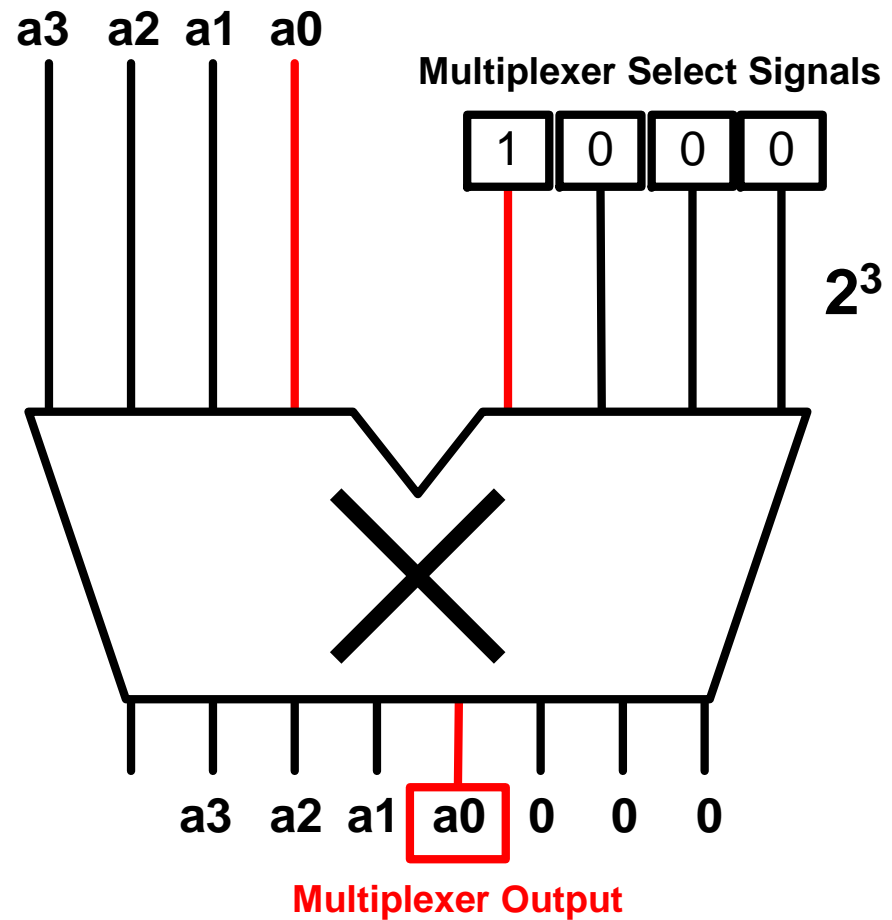
# Use Multiplier to Shift/Select

- Use shift to select input to pass through



# Use Multiplier to Shift/Select

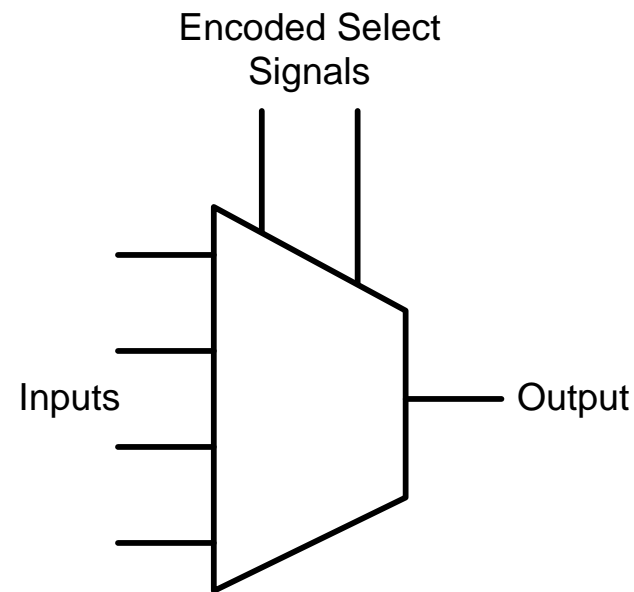
- Use shift to select input to pass through



# Doesn't look like a multiplexer

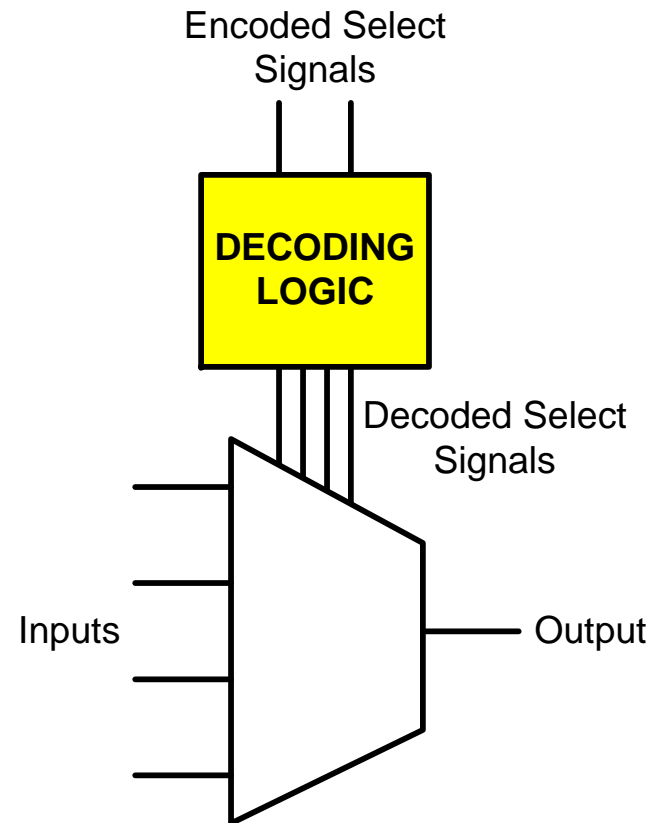
What we know:

- Multiplexer has encoded select signals



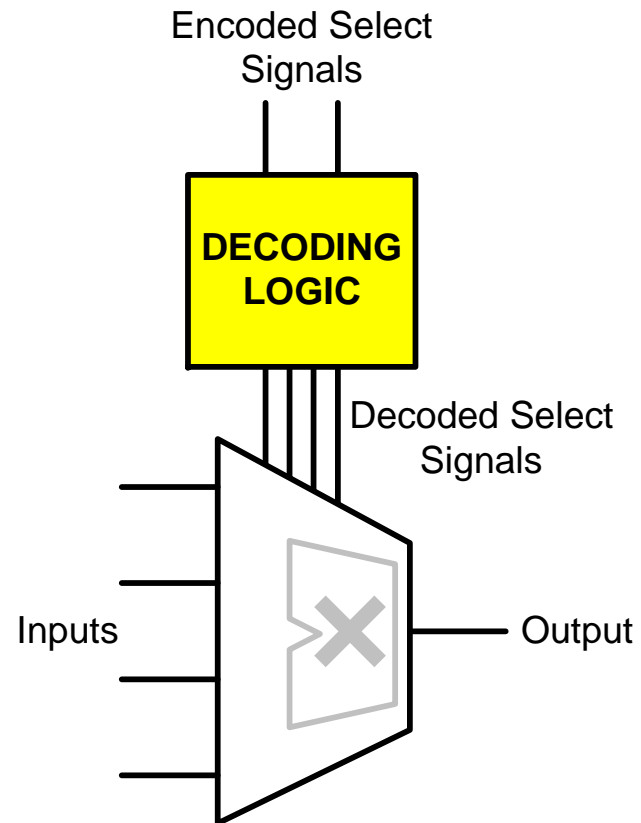
# Multiplier select Requires Decoded Selects

- Multiplier is only used to select signal
- Requires that select signals are decoded in programmable logic



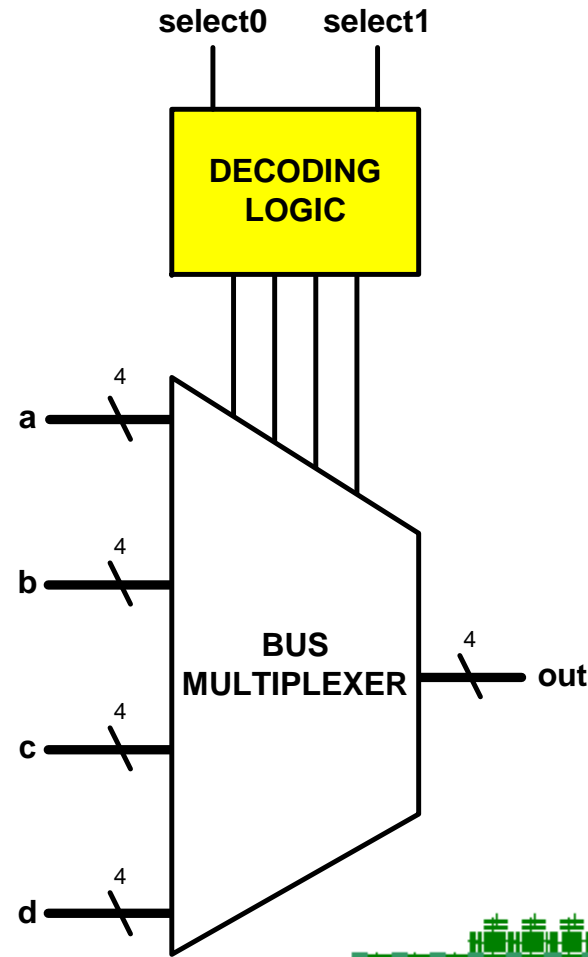
# Multiplier select Requires Decoded Selects

- Multiplier is only used to select signal
- Requires that select signals are decoded in programmable logic
- **Decoding costs**, but ...



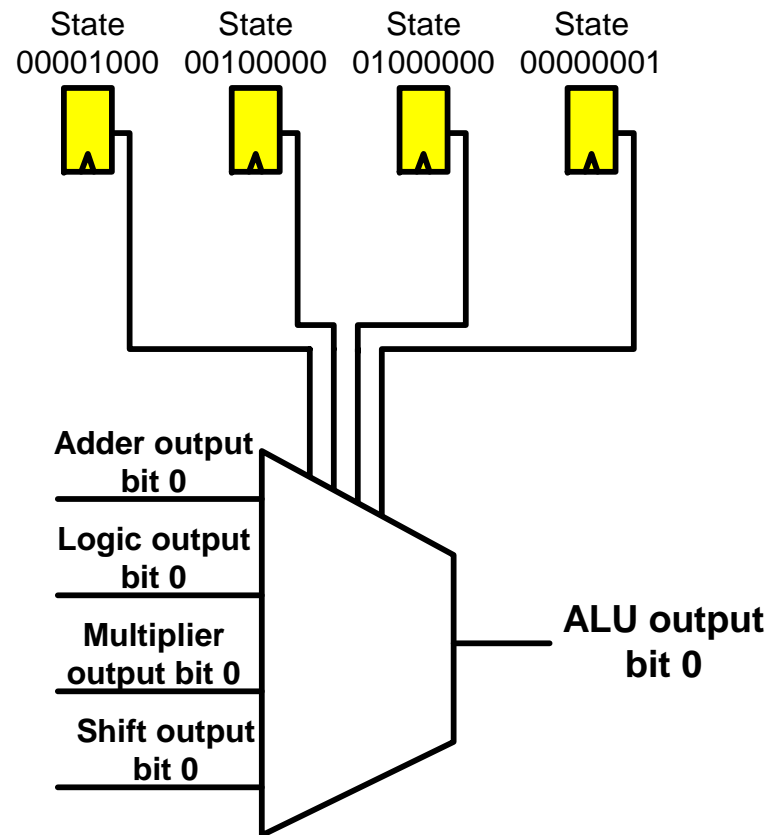
# 1. Can Amortize Decoding Logic

- For busses share signals to multiplex
- Only need to generate decoded selects **once**



## 2. Decoded Selects are Already There!

- Imagine a one-hot encoded state machine controlling the output of an ALU







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# Issue: Speed

- How will mapping affect circuit speed?
  - Example: 9:1 multiplexer
    - Soft logic mux = 422 MHz;
    - Built with 9\*9 hard multiplier = 307 MHz.
    - **115 MHz** slowdown!
- Problem if employed on critical path, or causes path to become critical





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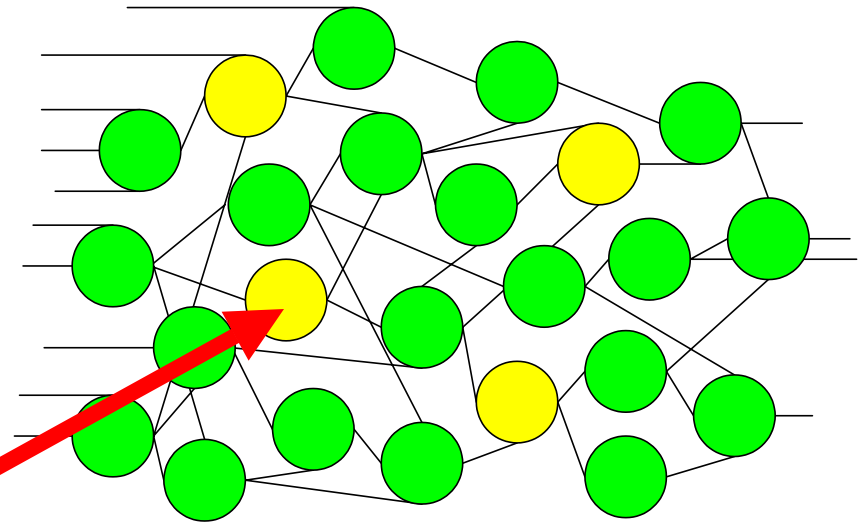
# Mapping Algorithm



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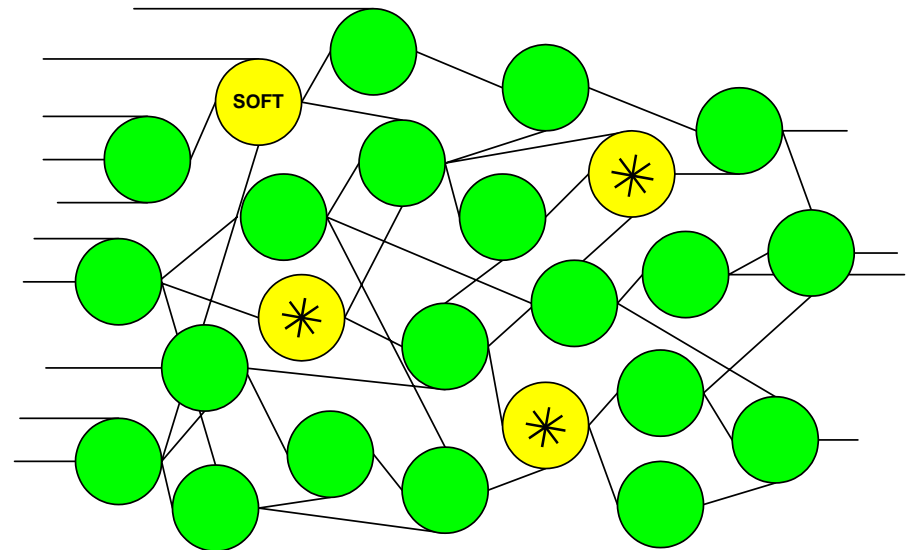
# Input

- Netlist of gates and some higher level structures
  - Logic
  - Multipliers
  - Memories
  - Multiplexers



# Output

- Similar netlist with multiplexers mapped to
  - hard multipliers or
  - soft logic





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# Goal of Algorithm

- Largest reduction in number of soft logic elements used
  - Potentially allow user to reduce part size, save money





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# Step 1


- Group all multiplexers that share common encoded select signals





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## Step 2

- For each group or multiplexer, estimate the area saving
    - Let
      - $CS(\text{size})$  = cost of implementing soft multiplexer
      - $CD(\text{size})$  = cost of decoding logic
      - $|M|$  = number of multiplexers in a group
    - $SAVINGS = (\sum CS(\text{size}) - CD(\text{size})) / |M|$
- 
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## Step 3

- Sort the groups and multiplexers in the order from greatest savings to least savings







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## Step 4

- Remove from list multiplexers on path that includes a multiplier
  - Hard multipliers often sit on critical path
  - Heuristic avoids speed reduction





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## Step 5

- Greedily select most-beneficial multiplexers to map
- Go back to step 4
- Finish
  - when no unused multipliers left
  - When no multiplexers left to map





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# Experimental Setup



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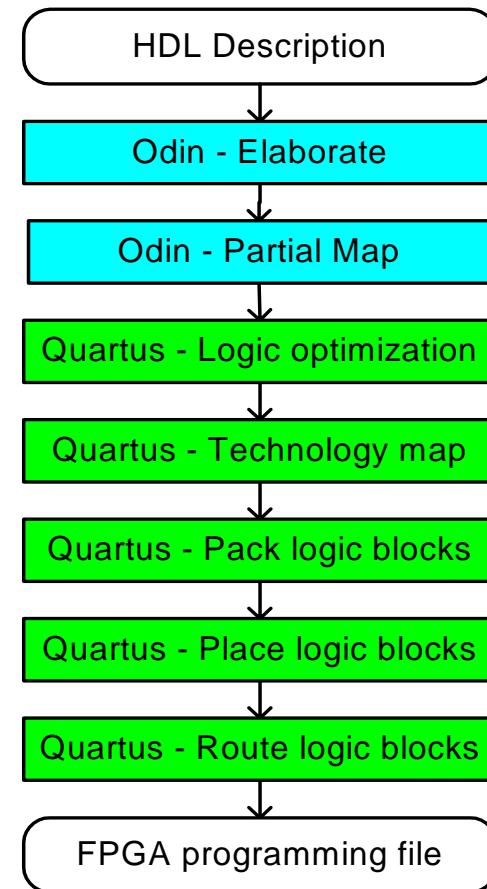
# Experimental Setup

- Will compare with and without mapping
- FPGA Used: Stratix I
- CAD Flow based on Altera Quartus 4.1



# CAD Flow

- New front-end synthesis
  - Odin [FPL 2005]
- Plugs into Quartus back-end from logic synthesis down





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# Benchmarks

- Collection of Verilog Benchmarks
  - Opencores
  - SCU-RTL
  - Texas-97
  - Benchmark Suite for Placement-2001
  - Local designs converted from VHDL
    - Raytrace
    - Molecular Dynamics
    - Stereo Vision
- Results are dependent on these benchmarks





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# Results

- Will present results separately for benchmarks with and without multipliers





# Results – Benchmarks without Multipliers

Benchmarks	Percent reduction in LEs	Percent Speed Gain
cordic_8_8	4%	-149%
cordic_18_18	1%	-25%
MAC1	5%	-40%
MAC2	2%	-12%
des_area	18%	5%
des_perf	5%	-145%
sv_chip0	1%	-30%
sv_chip0_no_mem	1%	-46%
sv_chip3_no_mem	19%	-168%
rt_frambuf_top	9%	-58%
rt_frambuf_top_no_mem	1%	-76%
rt_boundtop	2%	-31%
rt_boundtop_no_mem	5%	-33%
Geometric Average	6%	-54%

- Average reduction in LEs: 5.8%
- Average reduction in speed: 54%







# Results – Benchmarks with Multipliers

Benchmarks	Percent reduction in LEs	Percent Speed Gain
fft_258_6	1%	1%
iir1	0%	1%
iir2	11%	-1%
fir_3_8_8	0%	0%
fir_24_16_16	0%	0%
fir_scu_rtl	42%	-13%
diffeq_f_systemC	7%	0%
diffeq_paj_convert	12%	0%
sv_chip1	0%	-1%
rt_raygentop	5%	3%
rt_raygentop_no_mem	5%	-3%
oc45_cpu	6%	5%
reed_sol_decoder1	8%	-1%
reed_sol_decoder2	5%	1%
md	0%	0%
Geometric Average	8%	0%

- Average reduction in LEs: 7.6%
- Average reduction in speed: %0.5





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# Summary

- Technique reduces Logic Element Count by 6.8% on average across all benchmarks
- Reduction in speed varies:
  - Benchmarks that already employ multipliers almost no loss in speed
  - Benchmarks w/o multipliers: 54% reduction





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# Future Work

- Technique should improve if we can estimate speed of circuit paths at front-end
- Should architect a better hard structure that are more widely usable

